

# CODING FOR DATA SECURITY IN DISTRIBUTED STORAGE SYSTEM

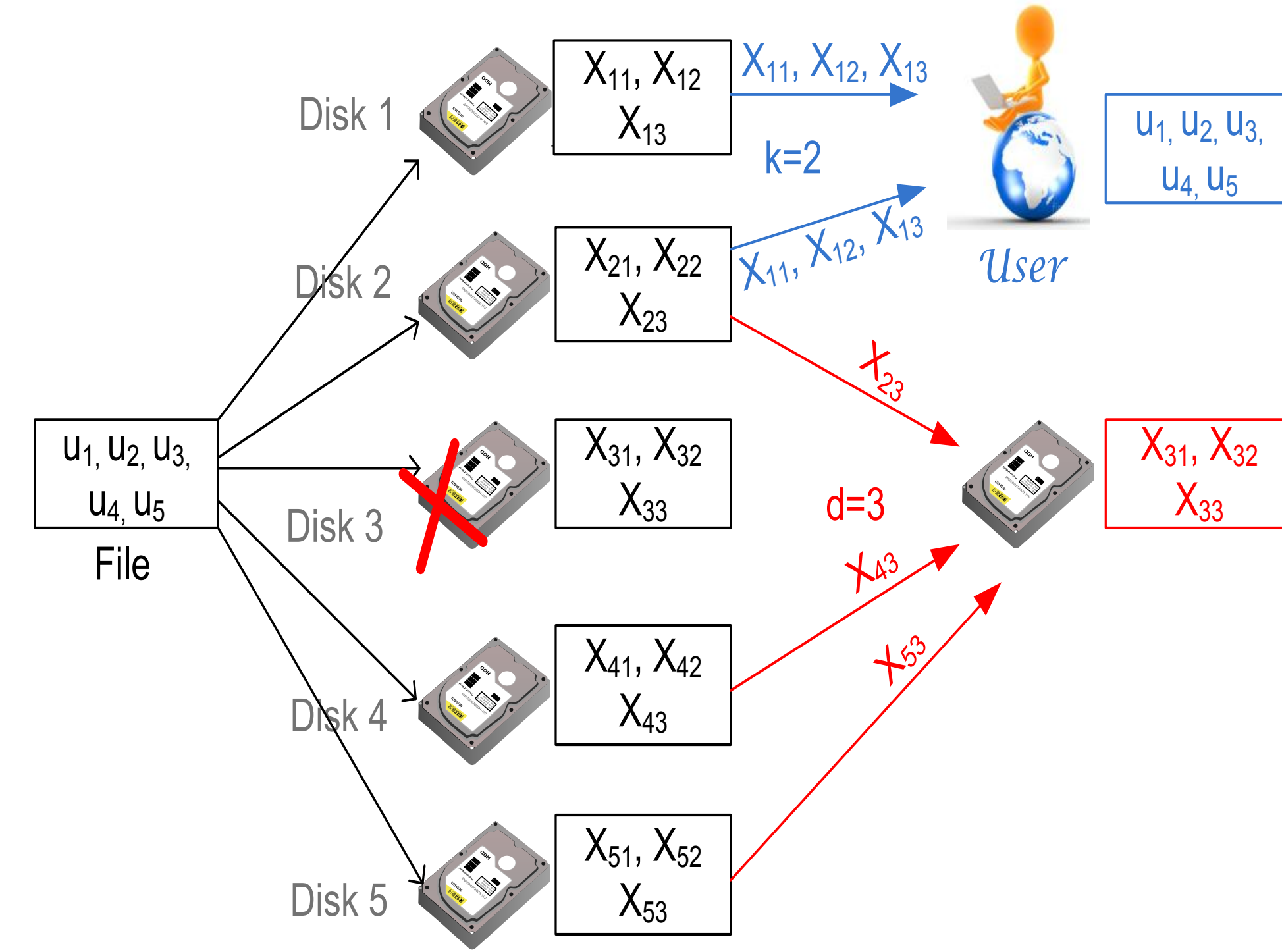
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## DISTRIBUTED STORAGE SYSTEMS

Distributed storage systems consist of storing data on  $n$  individually unreliable disks out of which any  $k$  are needed to reconstruct the stored data. In order to repair a failed disk,  $d$  disks are contacted.

To ensure these properties we use an  $(n, k, d)$  regenerating code [2].

With the introduction of regenerating codes, new tradeoffs and problems arise. For example by minimizing per disk storage, the bandwidth used to repair a failed disk increases. Trying to **secure** the system against **adversarial attacks**, the maximum file size is reduced. And the locality of the contacted disks used to repair other disks is also considered.



## RESULTS

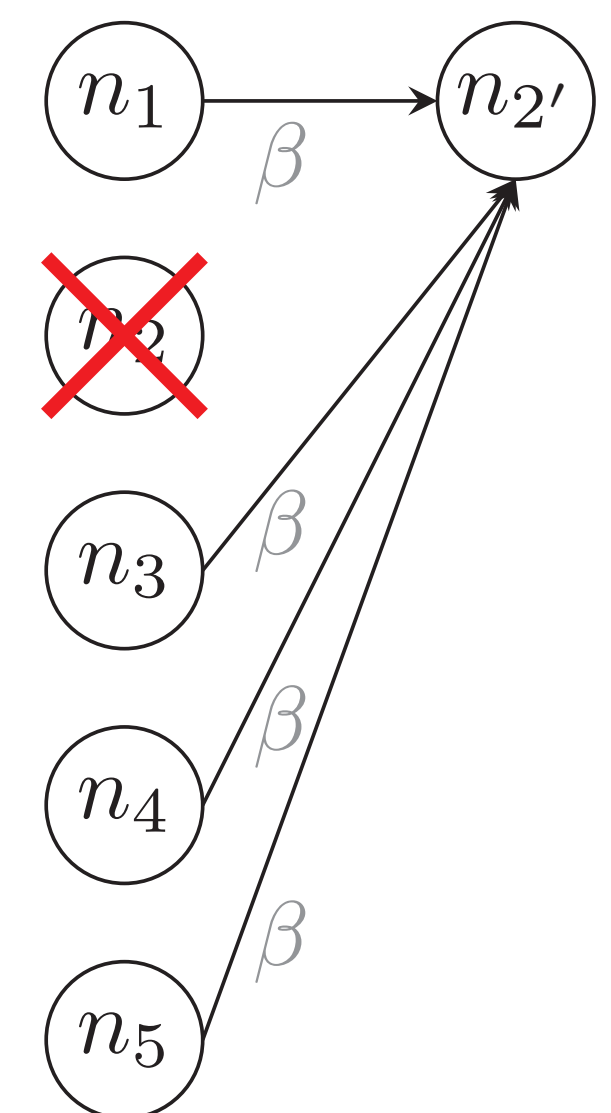
**Theorem 1** [1] An  $(n, k, d)$  regenerating code, operating in the bandwidth-limited regime, can be made resilient (with a small probability of error upper-bounded by  $\frac{1}{q}$ ) against an active limited-knowledge adversary controlling  $b < \frac{k}{2}$  nodes; and achieves with equality the resiliency capacity

$$C_r \leq \sum_{i=b+1}^k \min\{\alpha, (d-i+1)\beta\}.$$

**Theorem 2** The resilient  $(n, k, d)$  regenerating code can be made secure against Eavesdroppers controlling a subset  $l$  of the  $b$  nodes, achieving a maximum file size

$$M_{rs} \leq \sum_{i=l+b+1}^k \min\{\alpha, (d-i+1)\beta\}.$$

## SYSTEM'S PARAMETERS



An  $(n, k, d)$ -DSS storing data file  $\mathcal{F}$  of  $M$  symbols in  $\mathbb{F}_{q^v}$   
 $n = 5$ : total # of nodes  
 $k = 3$ : # min nodes to reconstruct  
 $d = 4$ : # helper nodes  
 $\alpha$ : storage per node  
 $\beta$ : repair bandwidth

**Reconstruction property:** any  $k$  out of  $n$  disks can recover  $\mathcal{F}$ .

**Exact repair property:** any  $d$  out of  $n$  disks can repair a failed disk by sending data less than  $M$ .  
 exact repair  $\implies$  Recover an exact copy of the lost data.

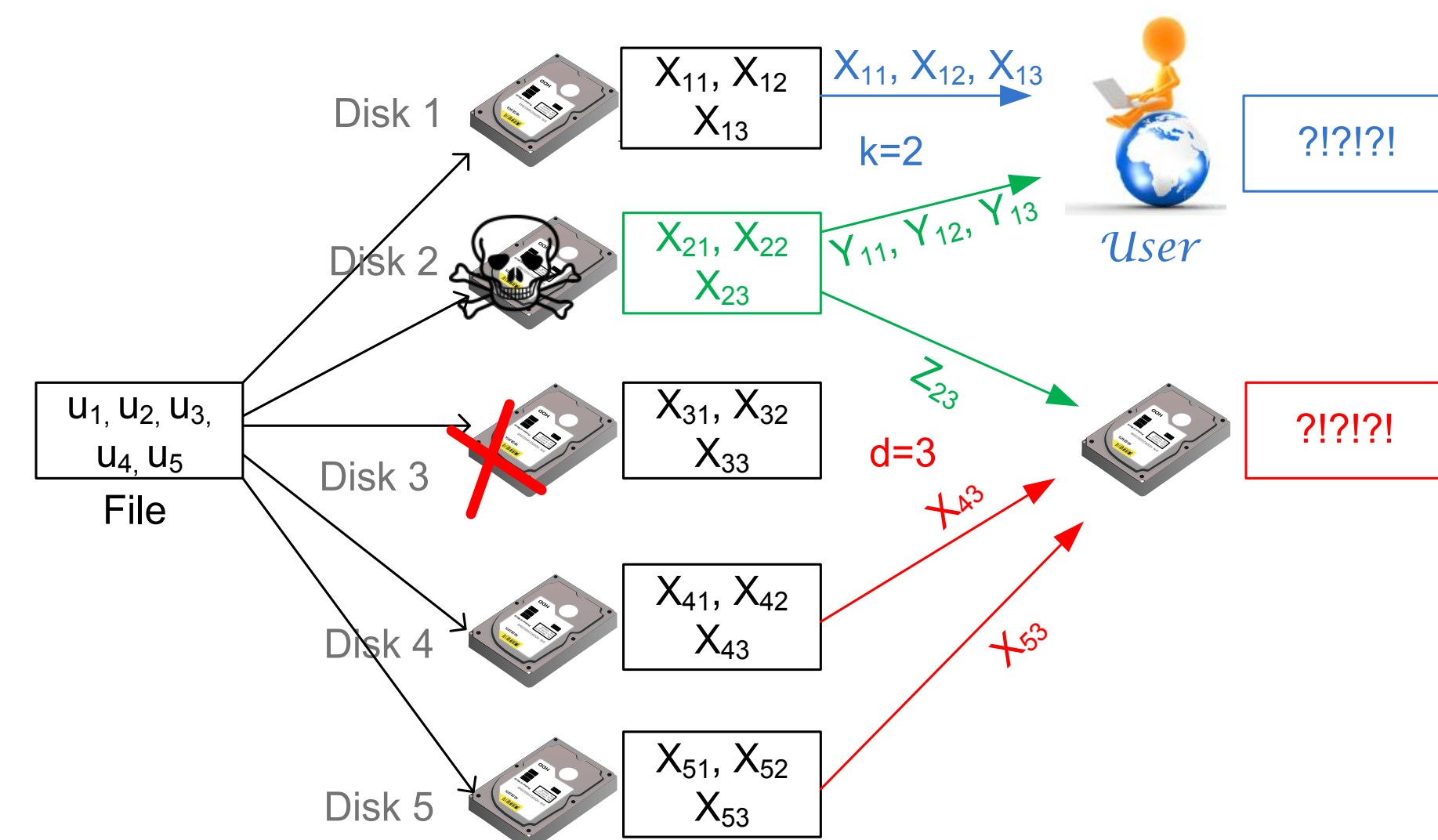
**Optimal repair bandwidth** [2]:

$$\beta = \frac{\alpha}{d} = \frac{\alpha}{4}.$$

In contrast to erasure codes such as Reed-Solomon, regenerating codes allow the system to repair a disk failure by downloading  $d\beta < M$  symbols.

## SECURITY PROBLEM

The **adversary** can observe and possibly corrupt the data on  $b$  nodes. If observing a replacement node, say  $n_2'$ , he can observe the repair data used to replace  $n_2$ .



**Resiliency capacity:**

Given an  $(n, k, d)$ -DSS with  $b$  compromised nodes, its *resiliency capacity*  $C_r(\beta)$  is defined to be the maximum file size that can be stored in the DSS, such that the reconstruction and the repair property will simultaneously hold.

**Upper bound** [3]

$$C_r \leq \sum_{i=b+1}^k \min(\alpha, (d-i+1)\beta).$$

**Perfect secrecy:** In some applications we also want to hide the data from the adversary.

## CAPACITY ACHIEVING CODE CONSTRUCTION

To secure an  $(n, k, d) = (5, 3, 4)$  DSS we build an  $(n, k-b, d-b) = (5, 2, 3)$  DSS, transform it into uncoded-repair. By contacting  $b$  more nodes and detecting the corrupted data using a hashing scheme we ensure a safe reconstruction and repair.

**Transforming the PM construction** [4] into uncoded repair

disk 1	$X_{12}$	$X_{13}$	$X_{14}$	$\{X_{15}\}$
disk 2	$X_{21}$	$X_{23}$	$X_{24}$	$\{X_{25}\}$
disk 3	$X_{31}$	$X_{32}$	$X_{34}$	$\{X_{35}\}$
disk 4	$X_{41}$	$X_{42}$	$X_{43}$	$\{X_{45}\}$
disk 5	$X_{51}$	$X_{52}$	$X_{53}$	$\{X_{54}\}$

**Hash function as introduced in** [3]: By abuse of notation we look at  $X_{ij} \in \mathbb{F}_{q^v}$  as a vector  $X_{ij} \in \mathbb{F}_q^v$ . We compute the dot product  $X_{ij} \cdot X_{lk} = \sum_{s=1}^v X_{ij}^s X_{lk}^s$  for  $ij \neq lk$  where  $X_{ij}^s \in \mathbb{F}_q$  and store them on a trusted server that can not be controlled by the adversary.

**Adversary detection during disk repair:**

	$X_{12}$	$X_{32}$	$X_{42}$	$X_{52}$
$X_{12}$		$\times$	$\checkmark$	$\checkmark$
$X_{32}$	$\times$		$\times$	$\times$
$X_{42}$	$\checkmark$	$\times$		$\checkmark$
$X_{52}$	$\checkmark$	$\times$	$\checkmark$	

**Adversary detection during file reconstruction:**

		disk 3			disk 2		
		$X_{31}$	$X_{32}$	$X_{34}$	$X_{21}$	$X_{23}$	$X_{24}$
disk 1	$X_{12}$	$\times$	$\times$	$\times$	$\checkmark$	$\checkmark$	$\checkmark$
	$X_{13}$	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$
	$X_{14}$	$\times$	$\times$	$\times$	$\checkmark$	$\checkmark$	$\checkmark$
disk 2	$X_{21}$	$\times$	$\times$	$\times$			
	$X_{23}$	$\checkmark$	$\checkmark$	$\checkmark$			
	$X_{24}$	$\times$	$\times$	$\times$			
disk 3	$X_{31}$				$\times$	$\checkmark$	$\times$
	$X_{32}$				$\times$	$\checkmark$	$\times$
	$X_{34}$				$\times$	$\checkmark$	$\times$

## REFERENCES

- [1] R.Bitars, S. El Rouayheb, "Securing data against Limited-Knowledge Adversaries in Distributed Storage Systems", submitted to IEEE International Symposium on Information Theory (ISIT), 2015.
- [2] A. Dimakis, P. Godfrey, Y. Wu, M. Wainright, and K. Ramchandran, "Network coding for distributed storage systems," *IEEE Transactions on Information Theory*, vol. 56, no. 9, pp. 4539–4551, 2010.
- [3] S. Pawar, S. El Rouayheb and K. Ramchandran, "Securing Dynamic Distributed Storage Systems Against Eavesdropping and Adversarial Attacks", *Information Theory*, IEEE Transactions on (Volume:57, Issue: 10), Oct 2011.
- [4] K. V. Rashmi, N. B. Shah, and P. V.Kumar, "Optimal Exact-Regenerating Codes for Distributed Storage at the MSR and MBR Points via a Product-Matrix Construction", *Information Theory*, IEEE Transactions on (Volume:57, Issue: 8), Aug 2011.
- [5] K. V. Rashmi, N. B. Shah, K. Ramchandran and P. V. Kumar, "Regenerating Codes for Errors and Erasures in Distributed Storage", *Information Theory Proceedings (ISIT)*, 2012 IEEE International Symposium, Jul 2012.